COVID-19: Reduced forms have gone viral, but what do they tell us?

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COVID 19: Reduced forms have gone viral, but what do they tell us?

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We explicit the link between epidemiological theory and reduced form estimations to assess the impact of mitigation policies on health outcomes. We identify three main caveats. First, reduced forms are subject to an omitted variable bias and consequently fail to estimate causal treatment effects. Second, identifying relevant control groups in the early stages of the epidemic is challenging. Third, agnostic reduced forms are of limited relevance to extrapolate the mid to long-run consequences of mitigation policies. Via simulations, we find that the omitted variable bias is potentially sizable and may result in misleading policy conclusions.

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The current COVID-19 pandemic poses a major and global health issue. As most non-pharmaceutical interventions to contain the pandemic involve an economic slowdown and a restriction of individual liberties, governments are facing an uneasy trade-off between the health benefits and the economic costs that these policies entail. Lockdown policies, in particular, may come at a high economic cost. Given the stakes, rigorously assessing the effectiveness of such policies is critical.

Multiple studies in the economics literature have relied on two-way fixed effects linear models to assess the causal impact of various mitigation policies on health outcomes. These studies rely on the spatial heterogeneity and timing of policy responses to identify treatment effects. They typically take the following form:

\[
\text{(1)} \quad \log(\text{confirmed cases}) = \text{policy} + \text{controls} + \text{fixed effects} + \text{error}
\]

As such methods are usually not grounded into epidemiological theory, we refer to them as agnostic reduced forms. This paper shows, both theoretically and on simulated data, that agnostic reduced-forms generally fail to identify treatment effects and deliver a sensible counterfactual analysis.

To make our case, we consider the Susceptible-Infected-Recovered-Deceased (SIRD) model as a benchmark for epidemic dynamics and derive a simple framework to think of policy evaluation in this context. Somewhat abusively, the observable inflow of new confirmed cases at each period may be written:

\[
\text{(2)} \quad \text{confirmed cases} = \text{tests} \times \text{contacts} \times \text{policy} \times \text{infected} \times \text{susceptible}
\]

Equation (2) has one major implication for reduced forms captured by Equation (1). As both the number of infected and susceptible individuals are unobserved and correlated to explanatory variables, agnostic reduced forms are subject to an omitted variable bias. It produces erroneous estimates of treatment effects, as well as uninterpretable geography and time fixed effects. In turn, resulting
counterfactuals may suggest misleading policy conclusions.\textsuperscript{1}

To get a sense of the magnitude of the bias, we simulate datasets from a SIRD data-generating process. In our simulations, we allow for a direct decreasing effect of mitigation policies on the contact rate. We also allow for a behavioral response of the population, which is unrelated to the policy implementation.\textsuperscript{2} All other endogeneity channels are shut down: there are no spillovers, the timing of mitigation policies is random and testing capacity is constant across geographical units and over time. We thus consider the ‘best of worlds’. We find that difference in differences as well as event studies fail to capture the true effect of the policy, in magnitude and sometimes even in sign. Though synthetic controls rely on a different empirical specification, they also largely fail to reconstruct a sensible counterfactual.

In addition, we highlight two additional caveats of reduced form estimations. First, identifying relevant control groups is challenging, as drastically different geographical units may display quite similar epidemic trends in the early stages of the epidemic. Second, since reduced form estimates are not closely tied to structural model parameters, they are of limited policy relevance to extrapolate the mid to long-run consequences of mitigation policies.

The rest of this paper is organized as follows. Section 1 reviews the literature. Section 2 discusses policy evaluation in the context of a pandemic. Section 3 focuses specifically on agnostic linear reduced forms and attempts to clarify their theoretical underpinnings. Section 4 presents simulation results. Section 5 addresses additional caveats of reduced form estimations. Section 6 concludes and discusses avenues for future research.

\textsuperscript{1}Our result does not stem from obvious threats to identification, such as spillover effects, endogenous timing of mitigation policies or variations in testing capacity over time.

\textsuperscript{2}This behavioral response may be thought of as a gradual change in behaviors as people learn to live with the threat of the disease.
I. Literature Review

Multiple studies in the economics literature rely on reduced form estimations to assess the causal impact of mitigation policies (e.g. face mask mandates, lockdowns) on health outcomes. They typically exploit the staggered implementation of mitigation policies across geographical units to estimate treatment effects and conduct counterfactual analysis. Most studies work with two-way fixed effects estimators (Hsiang et al., 2020; Dave et al., 2020; Fowler et al., 2020; Villas-Boas et al., 2020; Courtemanche et al., 2020; Lyu and Wehby, 2020; Karaivanov et al., 2020). Alternatively, a smaller set of papers relies on synthetic control methods (Friedson et al., 2020; Mitze et al., 2020). There is an apparent growing consensus that mitigation policies significantly reduce the spread of the disease. Though estimations vary drastically across settings and methodologies, the effects uncovered are generally sizable. For instance, Hsiang et al. (2020) estimate mitigation policies prevented (or delayed) approximately 61 million confirmed cases in a sample of six countries.

This paper provides two insights to this nascent literature. First, though resulting estimates have sometimes been interpreted as variations in the theoretical contact rate (Hsiang et al., 2020), we show that the link between agnostic reduced forms and epidemiological theory is tenuous. In fact, agnostic reduced forms are not related to the theoretical parameters of SIR-type models. Second, given that the focus of most studies has been on counterfactual analysis, we show that counterfactual exercises based on agnostic reduced forms are unreliable. In turn, previously established estimates should be interpreted with caution.

To bridge the divide between reduced-forms and structural approaches, recent contributions have combined structural econometrics with variants of SIR models to evaluate the efficiency of mitigation policies. On the one hand, Chernozhukov, Kasahara and Schrimpf (2021) outline a structural econometric model which explicitly assumes how information, policies and behavioral responses dynamically determine the spread of the disease. The resulting empirical specification is moti-
vated by the SIRD model, but ultimately makes different parametric assumptions. The authors highlight the importance of information and behavioral responses, but nonetheless conclude mitigation policies effectively reduced the spread of the disease in the United States. On the other hand, Allcott et al. (2020) explicitly combine a reduced-form estimation with a simplified SIRD model. They find modest mitigation policy effects and argue that most social distancing is driven by voluntary responses in the United States.

The latter study is closely related to this paper. The authors note that agnostic event studies may give bizarre results in the context of an epidemic, though they do not provide a formal theoretical explanation. This paper builds on their intuition and extends their observation to other types of reduced forms, such as general two-way fixed effects linear models and synthetic controls. We also provide a theoretical explanation for the poor performance of agnostic reduced forms in this context.

II. Policy Evaluation During a Pandemic

In this section, we introduce a simple model of epidemic dynamics and discuss the main threats to identification of treatment effects.

A. A Model of Epidemic Dynamics

Consider a discrete-time Susceptible-Infected-Recovered-Dead (SIRD) model (Kermack and McKendrick, 1927). Denote $S_t$, $I_t$, $R_t$, and $D_t$ the number of susceptible, infected, recovered, and deceased individuals at time $t$. The population may be written:

$$N = S_t + I_t + R_t + D_t$$
For all periods $t$, dynamics of the epidemic are modeled as follows:

\[
I_{t+1} = I_t + \beta_t S_t \frac{I_t}{N} - \gamma I_t \\
S_{t+1} = S_t - \beta_t S_t \frac{I_t}{N} \\
R_{t+1} = R_t + (1 - \mu) \gamma I_t \\
D_{t+1} = D_t + \mu \gamma I_t
\]

$\beta_t$ is the contact rate which captures the rate at which infected individuals transmit the disease to susceptible individuals in period $t$, $\gamma$ is the inverse of the recovery time for infected individuals and $\mu$ is the mortality rate of the disease. Epidemics usually display non-linear dynamics, which are determined by the time-varying basic reproduction number:

\[
R_{0t} = \frac{\beta_t}{\gamma}
\]

The contact rate $\beta_t$ is of particular interest, as it is likely an endogenous variable in the model. A change in the contact rate will change the shape of the entire epidemic curve for all subsequent periods in a non-linear fashion.

**B. Mitigation Policies and Confounding Factors**

Consider an analyst wishes to inform a policy maker on the impact of a dichotomous mitigation policy $P$ on health outcomes $Y(P)$. The policy’s causal effect may be thought of as $Y(1) - Y(0)$. The fundamental problem of causal inference is that $Y(1)$ and $Y(0)$ are not observed simultaneously for the same unit. The analyst’s main concern is therefore to find a counterfactual for $Y$ - which we denote $\hat{Y}(0)$ - for the treated unit (Rubin, 1974).

The mitigation policy’s primary objective is to decrease the contact rate, but little is known on other potential determinants of social distancing. We find it useful to think of $\beta_t$ as the product of an unknown function $G$, in which $X_t$ is
a vector of variables which could influence the population’s behavior (e.g. the number of recorded deaths, public medical information, disinformation on social media, government announcements), and the effect $\tau$ of a mitigation policy $P_t$: 

$$\beta_t = G(X_t) \exp(\tau P_t)$$

Though the analyst observes whether the policy was implemented, she does not know what would have been the contact rate without a policy implementation (as $G$ is unknown). In epidemiology, researchers sometimes assume that the contact rate would have remained the same without a policy implementation to conduct counterfactual analysis.\(^3\) This is a strong assumption and social scientists would expect behavioral responses unrelated to the mitigation policy. In turn, the analyst is likely to attribute part of the effects of changes in $X$ over time to the policy’s success or failure, as portrayed in Figure 1.

To overcome this issue, several reduced-form approaches have been used in the economics literature. Difference-in-differences and event studies compare outcomes of geographical units with a mitigation policy to geographical units without a mitigation policy over several time periods. Alternatively, synthetic control methods attempt to build a synthetic counterfactual for geographical units which implement a mitigation policy based on the observed outcomes of multiple geographical units which have not implemented such policies. Such methods could potentially account for changes in outcomes which are not attributable to the policy, and we thus study them in greater detail in the next section.

III. Epidemiological Theory and Agnostic Reduced Forms

In this section, we focus on agnostic linear models and their link with epidemiological theory. We show that agnostic reduced form estimations are subject to an

\(^3\)For example, Flaxman et al. (2020) write: ‘Our methods assume that changes in the reproductive number – a measure of transmission - are an immediate response to these interventions being implemented rather than broader gradual changes in behaviour.’
Figure 1: Treatment Effects and Confounding Factors

Notes: Figure 1 presents the evolution of an epidemic under three different scenarios: (1) a policy is implemented and there is an additional confounding factor; (2) no policy is implemented and there is an additional confounding factor; (3) no policy is implemented and there is no confounding factor. The confounding factor increases social distancing over time with or without a mitigation policy. If an analyst assumes no confounding factor for counterfactual analysis, then the third scenario may be thought of as the estimated counterfactual $\hat{Y}(0)$ for the first scenario $Y(1)$, and the second scenario may be thought of as the true counterfactual $Y(0)$. In this example, the analyst would largely overestimate the effect of the mitigation policy.
omitted variable bias, which in turn affects the identification of treatment effects and downstream counterfactual exercises.

A. General Specification

Denote $Y_{i,t}$ the outcome of interest for unit $i$ at time $t$, $E_i$ is the time for unit $i$ to initially implement a mitigation policy. $\delta_i$ and $\delta_t$ are respectively unit-specific and time fixed effects, and $\mathcal{E}$ is a set of intervals. Whether an analyst uses an event study or difference-in-differences, the specification will take the following general form:

\begin{equation}
Y_{i,t} = \alpha_0 + \delta_i + \delta_t + \sum_{g \in \mathcal{E}} \tau_g 1 \{ t - E_i \in g \} + \varepsilon_{i,t}
\end{equation}

B. Dependent Variables

Unfortunately, the contact rate, as well as the number of infected and susceptible individuals is generally unobserved. The analyst typically observes the number of confirmed infectious cases $C_t$ (and the number of deceased individuals $D_t$) as the epidemic unfolds. It is quite natural to use a transform of $C_t$ as a dependent variable, which we denote $Y_t$. In previous studies, the two preferred
dependent variables are:

(4) \[ Y_t = \log(C_t) \]

(5) \[ Y_t = \Delta \log(C_t) \]

Equation (4) is an approximation of the percentage change in confirmed cases \( C_t \), whereas Equation (5) is an approximation of the change in the growth rate from period \( t - 1 \) to period \( t \).

To link confirmed cases \( C_t \) with the SIRD model, we assume a proportional relationship between new infected individuals and confirmed cases in each period \( t \). Our main quantity of interest is therefore simply a proportion \( \theta_t \) of new infected individuals in period \( t \):

\[ C_t = \theta_t \beta_t S_t \frac{I_t}{N} \]

Previous contributions have assumed that \( C_t = \theta_t I_t \) (Chernozhukov, Kasahara and Schrimpf, 2021; Hsiang et al., 2020). This implies that infectious individuals could be tested positive more than once over the span of multiple time periods, which we deem unlikely in this context. Furthermore, in the SIRD model, new infected individuals is the only quantity which may be written as a linear combination when taking the log, and thus which does not violate the linearity assumption in linear regression models.

Note that \( C_t \) is often replaced by the number of deceased patients, \( D_t \). Since \( D_t \) is a function of infected individuals \( I_t \), the remarks from this paper also apply to dependent variables using a transform of deceased individuals (see appendix A for further details). For synthetic control methods, some studies have also worked with the cumulative number of confirmed cases:

\[ Y_t = \sum_{k=0}^{t} C_k \]

We assume that a fraction of newly infected individuals are directly tested positive in the same period. This is purely for clarity of exposition. We note that our results would remain unchanged if we were to specify a lag between the period of infection and the period of testing positive.
In the rest of this paper, we thus mainly focus on the log and the log-differences of $C_t$ as our dependent variable. To get a better sense of these dependent variables, let us decompose the log of new confirmed infectious cases. Assume that death and recovery rates are common to all geographical units and constant over time. Indexing geographical units by $i$, we may then write:

$$\log(C_{it}) = \log(\theta_{it}) + \log(G(X_{it})) + \tau P_{it} + \log(I_{it}) + \log(S_{it}) - \log(N_i)$$

According to an epidemiological data-generating process, the log of newly infected individuals is a function of testing capacity, of the current contact rate (potentially impacted by a mitigation policy), of the number of infected individuals, of susceptible individuals and of the population size for geographical unit $i$.

**C. The Omitted Variable Bias**

Equation (6) has a direct consequence for agnostic linear regression models captured by Equation (3). As the number of infected individuals $I_t$ and susceptible individuals $S_t$ are unobserved, reduced forms captured by Equation (3) cannot account for these quantities. Furthermore, both $I_t$ and $S_t$ are determined by the entire history of contact rates $\{\beta\}_t = \{\beta_0, \beta_1, ..., \beta_t\}$. Thus $I_t$ and $S_t$ are correlated to the policy dummy $P_t$. In turn, agnostic reduced forms are subject to an omitted variable bias and estimations will result in erroneous treatment effects.

In addition, this complicates the interpretation of time fixed effects common to all geographical units. As time dummies are also correlated to $I_t$ and $S_t$, they generally soak up part of the treatment effect. In turn, time fixed effects may not be interpreted as ‘the shape of the epidemic curve if there were no mitigation policy’ or simply as ‘shared temporal shocks across geographical units’.

6 A similar decomposition may be obtained for the approximation of growth rates:

$$\Delta \log(C_{it+1}) = \log\left(\frac{\theta_{it+1}}{\theta_{it}}\right) + \log\left(\frac{G(X_{it+1})}{G(X_{it})}\right) + \log\left(\frac{1 + \tau P_{it+1}}{1 + \tau P_{it}}\right) + \log\left(\frac{I_{it+1}}{I_{it}}\right) + \log\left(\frac{S_{it+1}}{S_{it}}\right)$$
The interpretation of geography fixed effects is also problematic. The contact rate $\beta$ affects non-linearly the entire shape of the epidemic curve. Different contact rates across regions will produce different epidemic dynamics. In turn, geography fixed effects may not control for \textit{ex ante} differences in contact rates across geographical units. This is true even if contact rates were to remain stable over time within geographical units.

Finally, the role of additional control variables is unclear in this context. Multiple studies condition on observables, such as socio-demographic characteristics (e.g. age structure, population, density), in an attempt to account for differences in epidemic dynamics across geographical units. Time-invariant characteristics may partly explain different \textit{ex-ante} contact rates, which will ultimately affect non-linearly the entire shape of the epidemic curve. In this case, as for geography fixed effects, specifying a linear term is unlikely to be a satisfactory work around. We leave this issue to future research.

IV. Simulations

In this section, we simulate a deterministic epidemiological model and assess different specifications based on their resulting counterfactual. As expected, agnostic linear models generally fail to identify treatment effects. In addition, the bias can be sizable.

A. Simulation Parameters and Functional Forms

We allow for (i) a policy intervention and (ii) an unrelated behavioral response of the population, which may be thought of as a time-varying confounding factor. For convenience, we assume that $\beta$ follows the following process:\footnote{Little is known on the typical behavioral responses of citizens during pandemics, and how these evolve with the epidemic outbreak. Note that the precise behavioral mechanism is of no importance for the purpose of this paper.}

\[
\beta_{it} = \beta_0 \exp\left(\delta_i + \tau P_{it} - \lambda t\right)
\]
\(\tau\) is the effect of the mitigation policy on the contact rate. In the absence of a mitigation policy, the contact rate decays exponentially over time at rate \(\lambda\). \(\delta_i\) are geography fixed effects which could capture cultural and/or socio-demographic \textit{ex-ante} differences in the population.\(^8\)

Data is simulated for 50 time periods. In our simplest example (difference-in-differences design), we simulate data for 2 geographical units. For all other examples, we simulate data for 50 geographical units. For difference-in-differences and the synthetic control, only one unit is treated in period 20. For event studies, all geographical units are eventually treated and the timing of treatment for each unit is drawn at random. In all cases, the policy reduces the contact rate by 20%.

Our simulated model abstracts from common endogeneity concerns expressed in the literature (refer to section V.A). Mitigation policies are implemented at random. Testing capacity is also fixed over time, across geographical units and equal to 1 (geographical units systematically detect all new infected individuals). Finally, there are no spillover effects. We investigate whether, in this ideal setup, agnostic reduced forms would perform as expected.

Additional details and figures for our simulations may be found in appendix B. We go through our main results in the Section IV.C.

\textbf{B. A Metric to Assess Specifications}

Policy makers are ultimately interested in comparing the estimated number of infected individuals over time with and without the implementation of a mitigation policy. As such, any viable specification should allow for a reasonably precise counterfactual analysis of these quantities. We thus compute a metric to assess the precision of the counterfactual in our simulations.

Denote \(Y(0)\) the number of confirmed cases if the geographical unit were not treated, \(\hat{Y}(0)\) its predicted value if it hadn’t been treated according to the fitted

\(^8\)As shown in Appendix C, confirmed cases in logs as well as in growth rates are remarkably different across US states in the early stages of the pandemic. In the SIRD model, such differences likely stem from \textit{ex-ante} differences in the contact rate across geographical units which we model via the geography fixed effects.
empirical model and \( T \) the total number of periods simulated.\(^9\) We define metric \( \mathcal{M} \) as:\(^{10}\)

\[
\mathcal{M} = \frac{1}{T} \sum_{t} \frac{|Y_t(0) - \hat{Y}_t(0)|}{Y_t(0)}
\]

Intuitively, \( \mathcal{M} \) captures to what extent the fitted empirical model is on average far from the true counterfactual value. The metric is normalized by the true counterfactual value to get a sense of the magnitude of the bias.

\[\text{C. Simulation Results}\]

We run difference-in-differences, event studies and synthetic control methods on our simulated datasets. Results for each empirical specification are presented in Table 1.\(^{11}\)

We make several observations for two-way fixed effects estimators. First, both differences-in-differences and event studies do not capture the mitigation policy’s effect on the theoretical contact rate. In this sense, they are not closely related to theoretical parameters in SIR-type models. Using the log of new infected individuals, difference-in-differences results in a large, negative and significant effect of the mitigation policy. When using log-differences, the effect of the mitigation policy is dwarfed. This is expected in theory, as a permanent decrease in the contact rate will only decrease the growth rate of new infections over one period. As the difference-in-differences specification assumes a constant treatment effect in the post-treatment period, the mitigation policy’s effect on growth rates is biased downwards.

Turning to event studies, both specifications in logs and log-differences seem to imperfectly capture the mitigation policy’s effect (See Figure 2), as estimates reflect a negative effect on logs as well as log-differences after the policy implemen-

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\(^9\)One advantage of simulating data is that we can always observe both \( Y(0) \) and \( Y(1) \).

\(^{10}\)Though our dependent variable is in logs or growth rates, we always translate into raw numbers of confirmed cases to compute the metric.

\(^{11}\)Appendix B presents each empirical specification. Further details, including figures of the raw data and coefficient estimates, may be found in the Online Appendix.
tation. However, confidence intervals are large despite the absence of noise in our simulations and seem to also capture spurious time trends in the pre- and post-treatment periods. As an element of comparison, we show the resulting estimates of theory-driven reduced forms, in which we control for the omitted variables in each specification.\textsuperscript{12}

As researchers may not be interested in recovering the mitigation policy’s effect on theoretical parameters, we also consider the accuracy of resulting counterfactuals. This leads us to our second observation: the $M$ metric is larger than zero in all specifications, which implies large differences between the predicted counterfactual $\hat{Y}(0)$ and the true counterfactual $Y(0)$. The metric ranges from an average 7\% up to 45\% discrepancy per period.

Regarding synthetic control methods, we find that such methods may produce unexpected results. The matrix completion method (Athey et al., 2018) fails to identify the sign of the mitigation policy’s effect. The generalized synthetic control (Xu, 2017) correctly captures the sign of the treatment effect, yet may produce very reliable counterfactuals, as reflected by a metric of 344\%.

V. Additional Issues

In this section, we address two additional issues related to agnostic reduced forms: choosing control groups and extrapolations.

A. What Makes for a Valid Control Group?

To estimate treatment effects, researchers typically use geographical units without a policy implementation as a control group for geographical units with a policy implementation as a treatment group. In the context of an epidemic, we note that valid control groups are hard to come by.

Researchers are aware of several limitations of their impact evaluation. We start with the three most common threats to identification which have been pre-
Table 1—: This table summarizes the results of the simulations. Estimates are displayed with the standard errors in between brackets. For "Event Study" specifications, the metric $M$ displayed is an average of each metric associated to a geographical unit. For additional details on our simulation results, see the Online Appendix.

<table>
<thead>
<tr>
<th>Specification</th>
<th>Outcome</th>
<th>Estimate</th>
<th>M Metric</th>
</tr>
</thead>
<tbody>
<tr>
<td>Difference-in-differences Logs</td>
<td>-0.28 (0.06)</td>
<td>0.07</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Rates</td>
<td>0.01 (0.01)</td>
<td>0.13</td>
</tr>
<tr>
<td>Event Study Logs See Figure 2</td>
<td>0.45</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Rates</td>
<td>See Figure 2</td>
<td>0.44</td>
</tr>
<tr>
<td>Generalized Synthetic Control</td>
<td>Cumulative -680361 (135554)</td>
<td>0.08</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Raw</td>
<td>-71985 (135554)</td>
<td>3.44</td>
</tr>
<tr>
<td>Matrix Completion Method Cumulative 1439814 (135554)</td>
<td>0.90</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Raw</td>
<td>85885 (135554)</td>
<td>0.76</td>
</tr>
</tbody>
</table>

Previously identified in the literature. First, variations over time and space of testing capacity may blur comparisons between and within groups. Second, the timing of mitigation policies could well be endogenous and depend on a geographical unit’s past health outcomes, economic circumstances and cultural preferences. Third, spillover effects are a likely scenario for mobile populations. Though these three confounding factors are important concerns to be addressed, they are not the focus of this paper. Instead, abstracting from these concerns, we ask what would theoretically be a valid control group for empirical analysis.

According to our epidemiological data-generating process, we find that common trends in a logs or growth rates of confirmed cases are demanding. In fact, different geographical units will follow similar epidemic trajectories if (1) the contact, recovery and death rates are equal for all geographical units at all periods and (2) the initial number of infected individuals as shares of the population are equal for all geographical units. In practice, this is unlikely to be the case, as any deviation for one of these parameters will have consequences on the entire shape of the epidemic curve.

In many applications, researchers investigate the validity of the common trends
Figure 2. : Event Study Estimates

Notes: This figure presents the results of event study specifications. Agnostic reduced forms are presented on the left column. Theory-driven reduced forms are presented on the right column. In the theory-driven specifications, we control for the relevant omitted variables. The first row displays the results for logs of new infections as the dependent variable. The second row displays the results for the delta logs of new infections as the dependent variable. The vertical dashed line corresponds to the last period before treatment occurs. Standard errors are clustered at the geographical unit level.

assumption in the pre-treatment period to assess the trustworthiness of their control groups. We note that apparent common trends may be misleading, notably in the early-stage of the epidemic. At the start of the outbreak the number of infected individuals is typically small and the susceptible population is close to the entire population size, which may blur ex-ante differences across regions (in particular if we were to add noise to the model). Figure 3 provides a graphical illustration. In such cases, a researcher could mistakenly attribute ex ante differences across geographical units to the success (or failure) of a mitigation
When it comes to growth rates, we note that similar epidemic trajectories necessarily have the same growth rates at each point in time. In this sense, the common trends assumption is not sufficient to conduct impact evaluation. On the contrary, non-zero geographical fixed effects are likely to be a strong indicator of \textit{ex ante} differences across geographical units. In the case of the United States, plotting the number of confirmed cases in logs or growth rates indicates potentially large \textit{ex ante} differences across geographical units (see appendix C).

![Figure 3](image)

**Figure 3.** An Example of Apparent Common Trends

**Notes:** This is a graphical example of misleading common trends in logs (left panel) and delta logs (right panel). Unit 1 (black line) has a baseline contact rate $\beta = 0.3$, whereas unit 2 (grey line) has a 20\% higher baseline contact rate than Unit 1. The treatment takes place at period 20 and has a null effect on the contact rate, yet trends of both units largely diverge in the post-treatment period.

**B. Short vs. Long Run Consequences of Mitigation Policies**

We raise one last drawback of agnostic reduced-forms: even if treatment effects were to be estimated without bias, they are only valid within the time window of the study. Yet, in the context of an epidemic, the number of averted infections at
a given point in time will likely greatly differ with the eventual number of averted infections by the end of the epidemic. A policy studied over a limited time horizon (say the early stages of the pandemic), will have weaker effects over the long run than estimated, because a fraction of infections are likely delayed rather than truly averted (hence the ‘flatten the curve’ narrative). Given healthcare capacity constraints, policy makers are certainly interested in the immediate effects of mitigation policies. Nonetheless, if policy makers are also interested in the number of infections averted by the end of the pandemic, agnostic reduced forms may not inform them on the impact of the mitigation policy outside of the study period considered.

VI. Conclusion

The COVID-19 pandemic has led to a vast research effort to provide policymakers with clear and reliable take-aways. Given the economic and social costs implied by several mitigation policies, rigorously assessing their effectiveness is critical. This paper sheds new light on the caveats of agnostic reduced-forms commonly used in the economics literature.

The core of our analysis is centered around the study of the SIRD model, which we see as a simple model to understand the dynamics of an epidemic. Based on theory, we raise several expected shortcomings of agnostic reduced-forms. They prove hard to interpret in light of epidemiological theory and are likely to produce unreliable counterfactuals. We then provide evidence of these shortcomings on simulated datasets. The bias can be sizable and could potentially lead to misleading policy conclusions. In addition, we note that identifying relevant control groups in the early stages of an epidemic is challenging. Finally, agnostic reduced forms are of limited relevance to inform policy-makers on the mid to long-run consequences of mitigation policies on health outcomes.

In many ways, these findings are reminiscent of old epistemological debates between theory-driven and agnostic approaches to data. When we correctly un-
derstand underlying mechanisms, theory may be useful and policy relevant. We conclude that a promising line of research is for economists to build causal frameworks upon the existing structural modeling literature in epidemiology.

REFERENCES


Villas-Boas, Sofia B, James Sears, Miguel Villas-Boas, and Vasco Villas-Boas. 2020. “Are We# StayingHome to Flatten the Curve?”


**Additional Technical Details on Dependent Variables**

In this appendix, we derive the anlytical expressions for deceased individuals according to our customized SIRD model.

*New Deceased Individuals (Logs)*

\[
\log(\Delta D_{it+1}) = \log(\mu) + \log(\gamma) + \log(N) + \log(C_t) - \log(\mathcal{G}(X_{it})) - \log(1 + \tau P_{it}) \\
- \log(S_{it}) - \log(\theta_{it})
\]

*New Deceased Individuals (Approximation of Growth Rates)*

\[
\Delta \log(\Delta D_{it+1}) = \log\left(\frac{C_{it}}{C_{it-1}}\right) - \log\left(\frac{\mathcal{G}(X_{it-1})}{\mathcal{G}(X_{it})}\right) - \log\left(\frac{1 + \tau P_{it-1}}{1 + \tau P_{it}}\right) \\
- \log\left(\frac{S_{it-1}}{S_{it}}\right) - \log\left(\frac{\theta_{it-1}}{\theta_{it}}\right)
\]
Additional Material for the Simulations

B1. Parameter Choices

Data is simulated for 50 time periods. In our simplest example (difference-in-differences design), we simulate data for 2 observational units of respective populations $10^5$ and $10^6$, with respective initial infected populations of 100 and 1,000. Treatment occurs in period 20. For all other examples (event studies and synthetic controls), we simulate data for 50 observational units. The size of the population is drawn from a uniform distribution $\mathcal{U}(10^6,10^7)$ and the share of initially infected individuals from a uniform distribution $\mathcal{U}(0.0001,0.001)$. We also allow for geography fixed effects drawn at random from $\delta_i \sim \mathcal{N}(0,0.1)$. For the synthetic control, only one unit is treated in period 20. For event studies, all geographical units are eventually treated and the timing of treatment for each unit is drawn from a uniform distribution $\mathcal{U}(0,50)$. In all cases, the policy reduces the contact rate by 20%.

The baseline contact rate is set to $\beta_0 = 0.3$. The learning parameter for the behavioral response is $\lambda = -0.002$ (i.e. we assume people ‘learn’ social distancing over time). Though, there is tremendous uncertainty on the values underlying epidemiological models in the context of the pandemic (Atkeson, 2020), the exact value is unlikely to matter for the purpose of this exercise. We consider $\gamma$ and $\mu$ as fixed over time (as there were no medical breakthroughs since the start of the COVID-19 pandemic) and choose reasonably plausible parameter values based on the literature. We set the inverse of the infection time $\gamma = 0.1$ and the death rate $\mu = 0.01$.

B2. Difference-in-differences

We run the following difference-in-differences specification on our simulated dataset:

$$Y_{it} = \alpha + \delta_i + \delta_t + \tau 1\{t > 19\} 1\{P_i = 1\} + \varepsilon_{it}$$
Geographical units are indexed by $i$ and time periods by $t$. $Y_{it}$ represents the outcome considered (logs and growth rates). $1\{t > 19\}$ is an indicator variable equal to 1 for the periods after the policy was implemented. $1\{P_i = 1\}$ equals to one for treated geographical units and 0 otherwise. $\delta_i$ and $\delta_t$ are respectively individual geography and common time fixed effects. $\tau$ is meant to capture the average treatment effect of the policy.

**B3. Event Study**

We run the following event study specification on our simulated dataset:

$$Y_{it} = \alpha + \delta_i + \delta_t + \sum_{k=-20; k \neq -1}^{k=20} \tau_k 1\{t - E_i = k\} + \varepsilon_{it}$$

Geographical units are indexed by $i$ and time periods by $t$. $Y_{it}$ represents the outcome considered (logs or growth rates). $1\{t - E_i = k\}$ is an indicator for the days relative to the first day of the mitigation policy considered $E_i$. $\delta_i$ and $\delta_t$ are respectively geography and time fixed effects. The first period before treatment occurs is taken as the baseline. Time periods before $k=-20$ and after $k=20$ are pooled in the $1\{t - E_i = -20\}$ and $1\{t - E_i = 20\}$ time indicators respectively.

**B4. Synthetic Controls**

Finally, we test the synthetic control methods proposed by Athey et al. (2018) and Xu (2017). To remain close to previous empirical applications, we use alternatively the cumulative number of new infected individuals or the raw number of new infected individuals as a dependent variable.
Comparison to Real Data (United States)

Figure C1. COVID-19 Confirmed Cases in the U.S.

Notes: This is a graphical overview of the US data, which may be freely downloaded at: https://covidtracking.com/data/download. Each line represents a US state. Each row plots respectively the raw number of new confirmed cases, new confirmed cases in logs and new confirmed cases in growth rates.